

- The domain of the function

$$\mathbf{r}(t) = \langle t^2, \sqrt{t-1}, \sqrt{5-t} \rangle$$

- The time at which the following two particles collide, if they do indeed collide; for $t \geq 0$, their paths are given by

$$\mathbf{r}_1(t) = \langle t^2, 7t-12, t^2 \rangle \quad \mathbf{r}_2(t) = \langle 4t-3, t^2, 5t-6 \rangle$$

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$$\lim_{t \rightarrow 1} \left(\sqrt{t+3} \mathbf{i} + \frac{t-1}{t^2-1} \mathbf{j} + \frac{\tan t}{t} \mathbf{k} \right)$$

- The derivative of $\mathbf{r}(t) = \langle \cos t, \sin t \rangle$.

- A parametric equation for the line segment that joins $(0,0,0)$ to $(1,2,3)$.

- The derivative of $\mathbf{r}(t) = e^{t^2} \mathbf{i} - \mathbf{j} + \ln(1+3t) \mathbf{k}$.

- A Daily Double! Sketch the curve with the equation $\mathbf{r}(t) = \langle t, \cos 2t, \sin 2t \rangle$.

- The unit tangent vector of the path $\mathbf{r}(t) = \cos t \mathbf{i} + 3t \mathbf{j} + 2 \sin 2t \mathbf{k}$ when $t = 0$.

- The parametric equations for the tangent line to the curve with the parametric equations
- (A Daily Double!) Sketch the graph of $f(x, y) = 1 - x^2$.

$$x = e^{-t} \cos t, \quad y = e^{-t} \sin t, \quad z = e^{-t}$$

at the point $(1, 0, 1)$.

- $\int (e^t \mathbf{i} + 2t \mathbf{j} + \ln t \mathbf{k}) dt$
- The contour map of $f(x, y) = x - y^2$ showing the level curves $z = -2, -1, 0, 1, 2$.

- $f(2, -1, 6)$ where $f(x, y, z) = e^{\sqrt{z-x^2-y^2}}$.

- A thin metal plate, located in the xy -plane, has temperature $T(x, y)$ at the point (x, y) . The level curves of T are called *isothermals* because at all points on an isothermal the temperature is the same. Sketch some isothermals if the temperature function is given by

- The approximate value for $f(-3, 3)$ given the contour map for f below:

$$T(x, y) = 100 / (1 + x^2 + 2y^2)$$

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$$\lim_{(x,y) \rightarrow (0,0)} \frac{x^2}{x^2 + y^2}$$

• The value of

$$\lim_{(x,y,z) \rightarrow (0,0,0)} \frac{xyz}{x^2 + y^2 + z^2}$$

(hint: use spherical coordinates).

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$$\lim_{(x,y,z) \rightarrow (3,0,1)} e^{-xy} \sin(\pi z/2)$$

• The partial derivatives $f_x(x, y)$ and $f_y(x, y)$ of the function $f(x, y) = xe^{3y}$.

• The points at which the function $F(x, y) = \sin(xy)/(e^x - y^2)$ is continuous.

• The partial derivative $f_z(x, y, z)$ of the function $f(x, y, z) = xy^2z^3 + 3yz$

• The value of

$$\lim_{(x,y) \rightarrow (0,0)} (x^3 + y^3)/(x^2 + y^2)$$

(hint: use polar coordinates).

• The partial derivative $\partial z/\partial x$ of the implicitly defined function $x^2 + y^2 + z^2 = 3xyz$.

- The second partials u_{xx} , u_{yy} , and u_{zz} of the function $u = 1/\sqrt{x^2 + y^2 + z^2}$. (Hint: they satisfy the three-dimensional Laplace equation $u_{xx} + u_{yy} + u_{zz} = 0$.)
- The equation of the tangent plane to the surface $z = y \cos(x - y)$ at the point $(2, 2, 2)$.

- (A Daily Double!) The kinetic energy of a body with mass m and velocity v is $K = \frac{1}{2}mv^2$. Show that

$$\frac{\partial K}{\partial m} \frac{\partial^2 K}{\partial v^2} = K$$

- The differential of $u = e^t \sin \theta$.

- The differential of $w = \ln \sqrt{x^2 + y^2 + z^2}$.

- The equation of the tangent plane to the surface $z = 4x^2 - y^2 + 2y$ at the point $(-1, 2, 4)$.
- The estimated maximum error in calculating the area of a rectangle of length 30 cm and width 24 cm (with an error at most 0.1 cm in each), using differentials.

- The derivative dz/dt where

$$z = x^2y + xy^2, \quad x = 2 + t^4, \quad y = 1 - t^3$$

- (A Daily Double!) The rate at which the temperature is rising on the bug's path after 3 seconds, where the bug is crawling along the path

$$x = \sqrt{1+t}, \quad y = 2 + \frac{1}{3}t$$

(x and y are measured in cm) starting at $t = 0$ seconds, and the temperature $T(x, y)$ at the point (x, y) satisfies $T_x(2, 3) = 4$ and $T_y(2, 3) = 3$.

- The derivative dw/dt where

$$w = xe^{y/z}, \quad x = t^2, \quad y = 1 - t, \quad z = 1 + 2t$$

- The partial derivative $\partial z/\partial s$ where $z = e^r \cos \theta$, $r = st$, $\theta = \sqrt{s^2 + t^2}$.

- The directional derivative of $f(x, y) = \sqrt{5x - 4y}$ at the point $(4, 1)$ in the direction $\theta = -\pi/6$.

- The partial derivative $\partial u/\partial \theta$, where

$$u = x^2 + yz, \quad x = pr \cos \theta, \quad y = pr \sin \theta$$

and $z = p + r$ when $p = 2$, $r = 3$, $\theta = 0$.

- The gradient of $f(x, y, z) = xe^{2yz}$.

- The directional derivative of the function $f(x, y) = 1 + 2x\sqrt{y}$ at the point $(3, 4)$ in the direction of the vector $\langle 4, -3 \rangle$.
- A pentagon is formed by placing an isosceles triangle on a rectangle, as shown in the figure. If the pentagon has fixed perimeter P , find the lengths of the sides of the pentagon that maximize the area of the pentagon.
- The equation of the tangent plane the surface $x^2 + 2y^2 + 3z^2 = 21$ at the point $(4, -1, 1)$.
- The points on the hyperboloid $x^2 - y^2 + 2z^2 = 1$ where the normal line is parallel to the line that joins the points $(3, -1, 0)$ and $(5, 3, 6)$.