

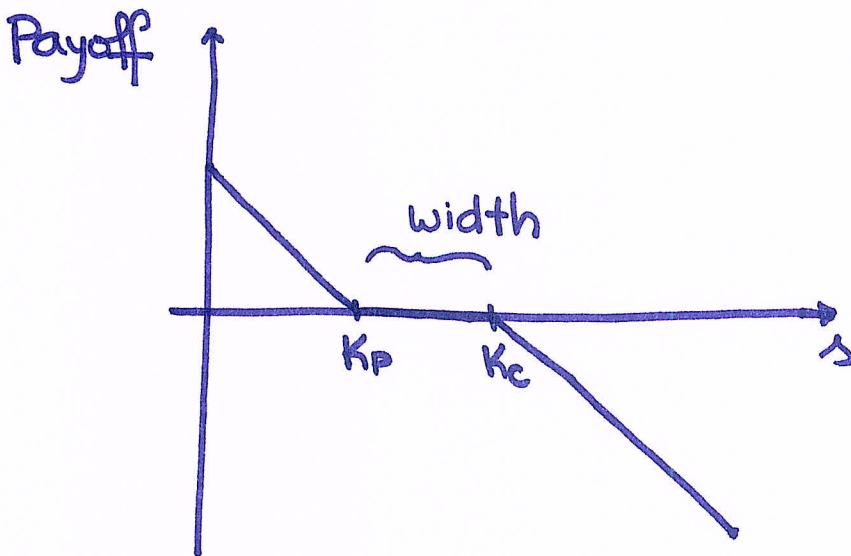
Ⓛ: April 5th, 2019.

Collars [review].

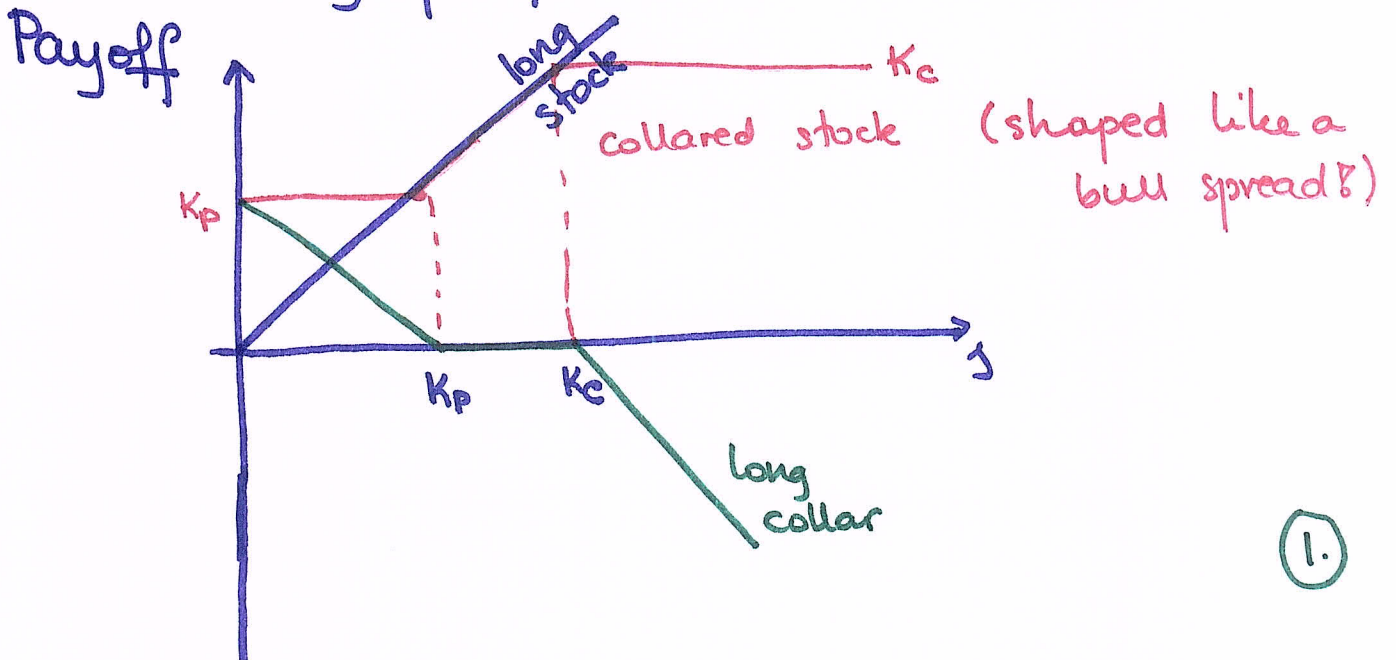
Let $K_p \leq K_c$.

{
• LONG the K_p -strike put
• WRITE/SHORT the K_c -strike call
}

European;
otherwise
identical



We use the long collar to hedge a long stock.
The resulting portfolio is a collared stock.

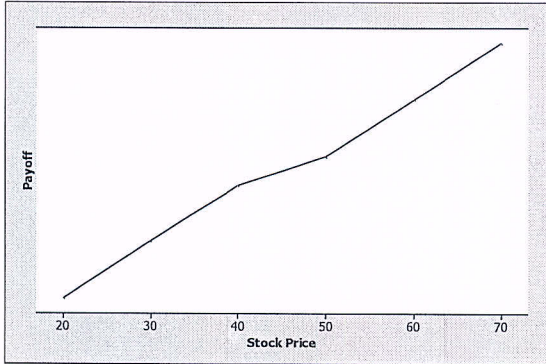


59.

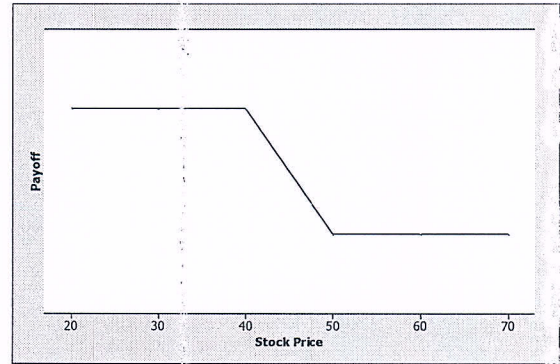
An investor has a long position in a non-dividend-paying stock, and additionally, has a long collar on this stock consisting of a 40-strike put and 50-strike call.

Determine which of these graphs represents the payoff diagram for the overall position at the time of expiration of the options.

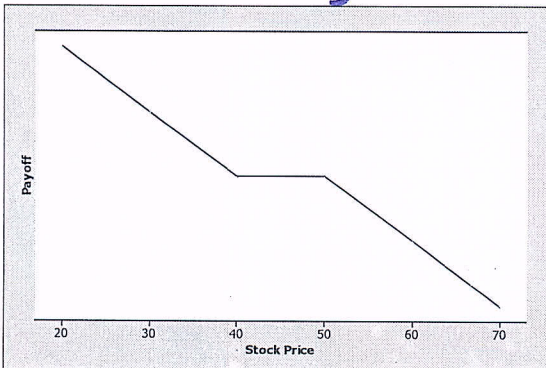
(A) X



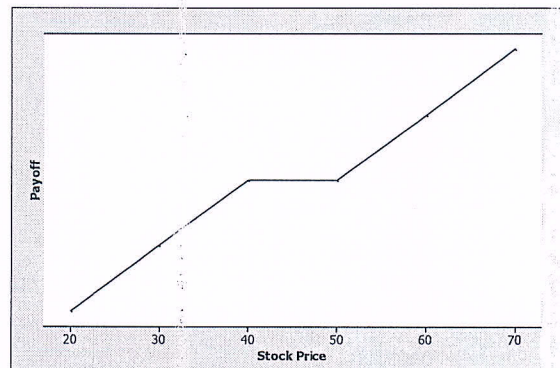
(B) bear spread + bond = short collared stock



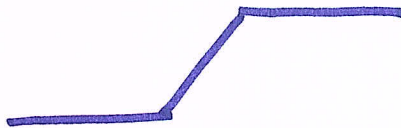
(C) "naked" long collar



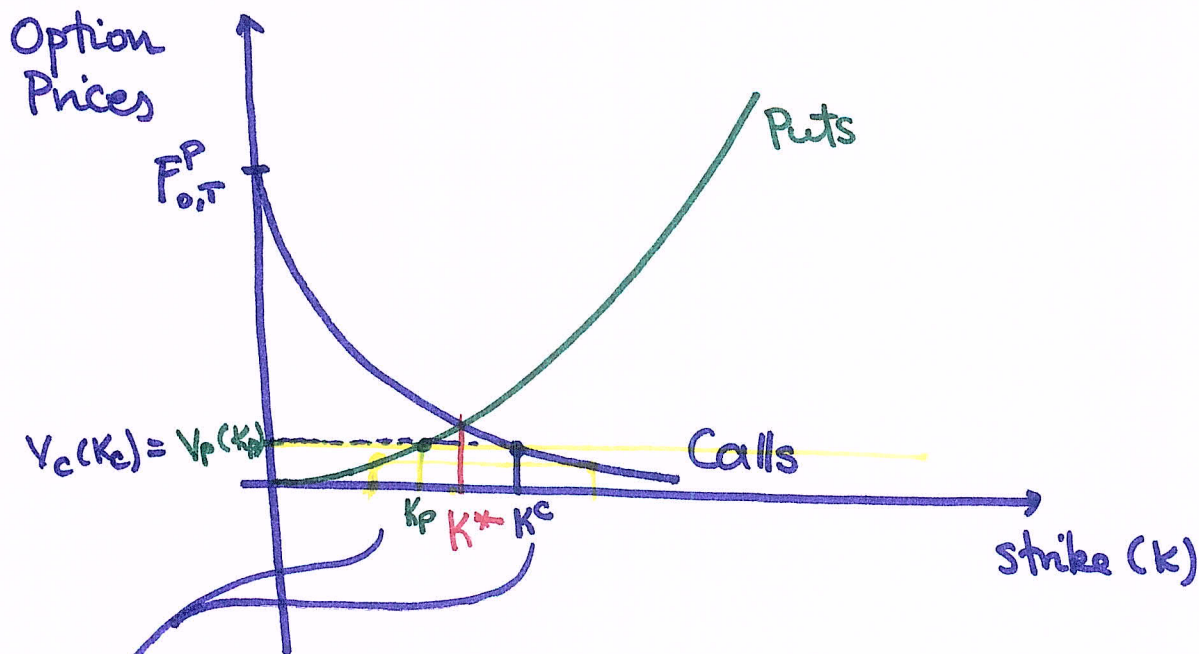
(D) "naked" short collar



(E) W



Zero-Cost Collars



By put-call parity:

$$0 = V_c(K^*) - V_p(K^*) \stackrel{\text{put-call parity}}{=} F_{0,T}^P - PV_{0,T}(K^*)$$

$$\Rightarrow F_{0,T}^P = PV_{0,T}(K^*)$$

$$\Rightarrow K^* = F_{0,T}$$

For each pair K_P & K_C obtained as above, we end up w/ a (K_P, K_C) -collar whose cost is **ZERO**.

We have infinitely many zero-cost collars.

Ratio Spreads.

Let $K_1 < K_2$

- LONG m calls w/ strike K_1
 - SHORT/WRITE n calls w/ strike K_2
- } European; otherwise identical

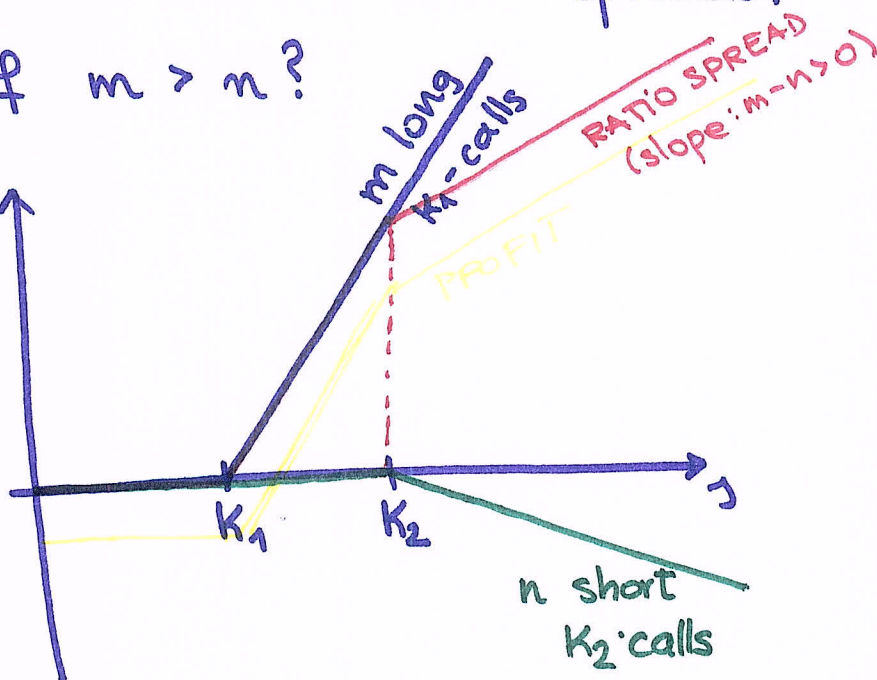
w/ m and n positive constants; usually integers.

Q: What if $m = n$?

It's like m call bull spreads.

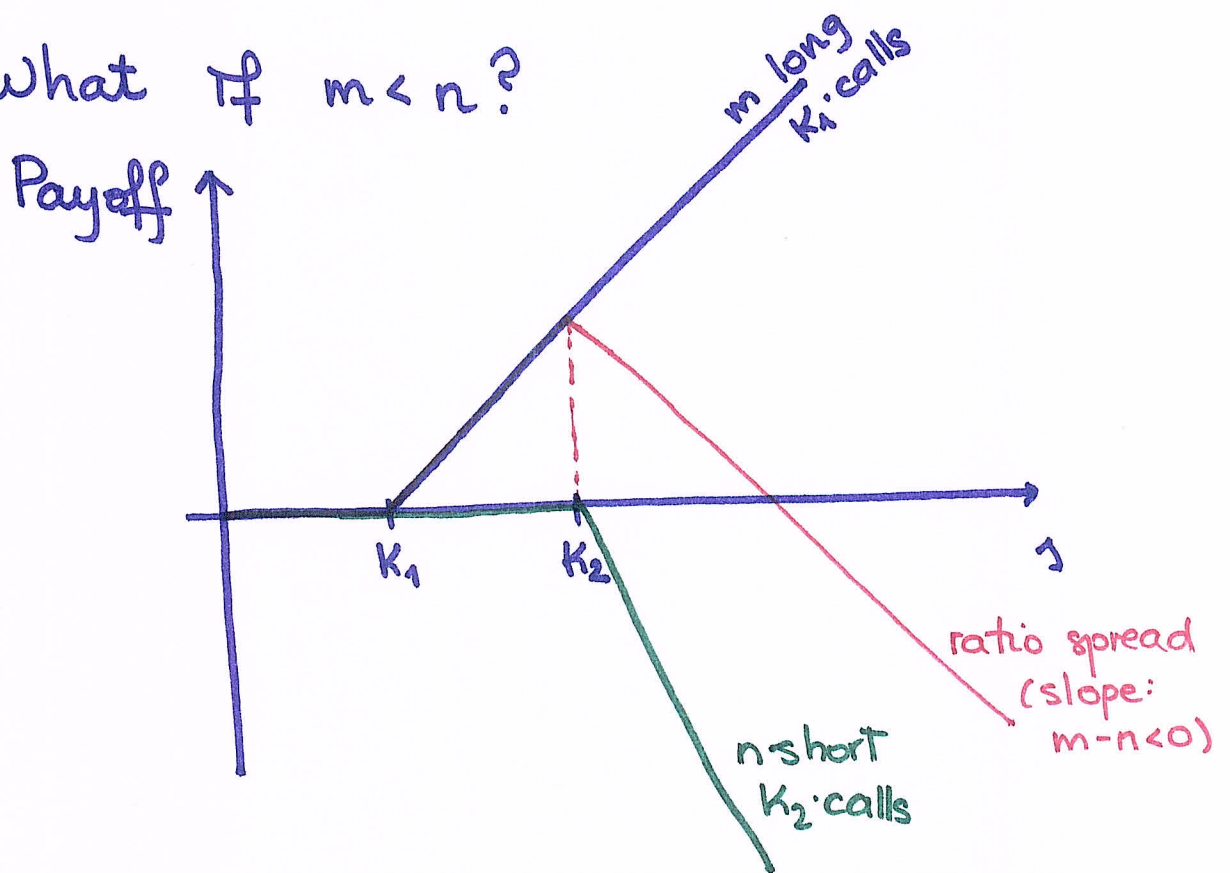
Q: What if $m > n$?

Payoff



- Q: Who would trade in this position?
- Speculators on higher prices.
 - Long w.r.t. the underlying
=> Use it to hedge a short position.

Q: What if $m < n$?



Q: Who would invest in this ratio spread?

- Arbitrageur X No lower bound!
- Speculator: Low volatility & low likelihood of high prices
- Hedger X No directionality!

38.

The current price of a medical company's stock is 75. The expected value of the stock price in three years is 90 per share. The stock pays no dividends.

You are also given

- i) The risk-free interest rate is positive.
- ii) There are no transaction costs.
- iii) Investors require compensation for risk.

The price of a three-year forward on a share of this stock is X , and at this price an investor is willing to enter into the forward.

Determine what can be concluded about X .

- (A) $X < 75$
- (B) $X = 75$
- (C) $75 < X < 90$
- (D) $X = 90$
- (E) $90 < X$

39.

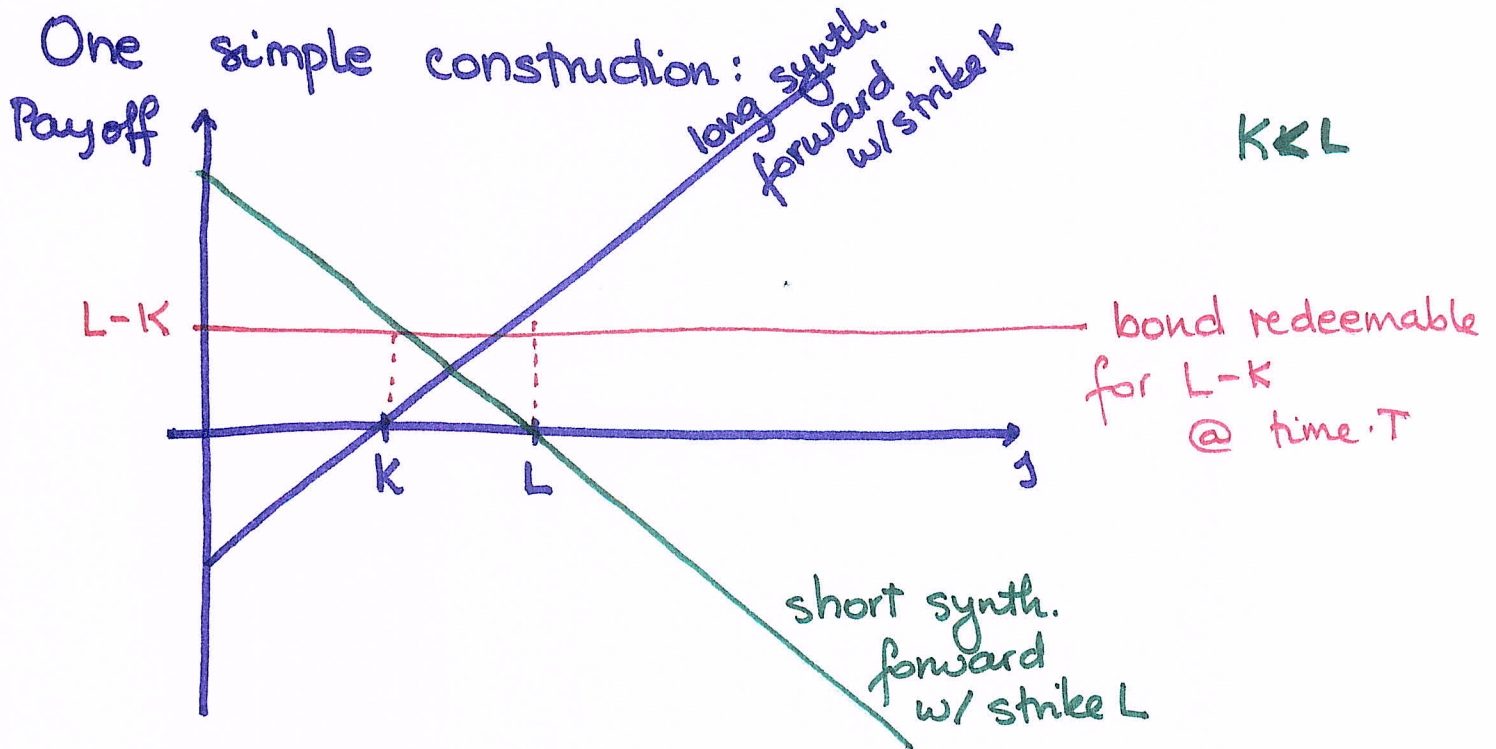
Determine which of the following strategies creates a ratio spread, assuming all options are European.

- calendar spreads*
- (A) Buy a one-year call, and sell a three-year call with the same strike price.
 - (B) Buy a one-year call, and sell a three-year call with a different strike price.
 - (C) Buy a one-year call, and buy three one-year calls with a different strike price.
 - (D) Buy a one-year call, and sell three one-year puts with a different strike price.
 - (E) Buy a one-year call, and sell three one-year calls with a different strike price. 😊

long call + long bond
"
long put + long stock

Box Spreads

... replicate a bond



Put-call Parity:

• long a K -strike call*
 • short a K -strike put*

LONG synthetic forward w/ strike K

• short an L -strike call*
 • long an L -strike put*

SHORT synthetic forward w/ strike L

Box Spread : {

- * LONG (K, L) -call bull spread
- * LONG (K, L) -put bear spread

 }

53.

For each ton of a certain type of rice commodity, the four-year forward price is 300. A four-year 400-strike European call option costs 110.

The continuously compounded risk-free interest rate is 6.5%.

Calculate the cost of a four-year 400-strike European put option for this rice commodity.

- (A) 10.00
- (B) 32.89
- (C) 118.42
- (D) 187.11
- (E) 210.00

54.

DELETED

55.

Box spreads are used to guarantee a fixed cash flow in the future. Thus, they are purely a means of borrowing or lending money, and have no stock price risk.

Consider a box spread based on two distinct strike prices (K, L) that is used to lend money, so that there is a positive cost to this transaction up front, but a guaranteed positive payoff at expiration.

Determine which of the following sets of transactions is equivalent to this type of box spread.

- (A) A long position in a (K, L) bull spread using calls and a long position in a (K, L) bear spread using puts.
- (B) A long position in a (K, L) bull spread using calls and a short position in a (K, L) bear spread using puts. $\uparrow \uparrow \times$
- (C) A long position in a (K, L) bull spread using calls and a long position in a (K, L) bull spread using puts. \times
- (D) A short position in a (K, L) bull spread using calls and a short position in a (K, L) bear spread using puts. **BORROWING!**
- (E) A short position in a (K, L) bull spread using calls and a short position in a (K, L) bull spread using puts. $\downarrow \downarrow \times$

Spreads etc.

+ hedging	call bull spreads	↑	≥ 0	arbitrage p.
	put bull	- - ↑	≤ 0	monot.
	call bear	- - ↓	≤ 0	conv slope
	put bear	- - ↓	≥ 0	monot.

butterfly spreads
+ speculation on low vol.

straddles + strangles
speculation on high vol

• collars

• ratio spreads

• box spreads —

convexity