Problem 3.1. (2 pts) Let the stock price $S(t)$ be modeled using the lognormal distribution. Define $Y(t) = S(t)^3$. Then, the random variable $Y(t)$ is lognormal itself. True or false?

Problem 3.2. (2 pts) Let the stochastic process $S = \{S(t), t \geq 0\}$ represent the stock price as in the Black-Scholes model. Let its volatility term be denoted by $\sigma$. Then, the volatility parameter of the process $Y(t) = 2S(t)$ is $4\sigma$.

Problem 3.3. (2 pts) 
Theta may also be called time decay. True or false?

Problem 3.4. (5 pts) Which of the following gives the correct values for the delta and gamma of a single share of non-dividend-paying stock?
(a) $\Delta = 1, \Gamma = 1$
(b) $\Delta = 1, \Gamma = 0$
(c) $\Delta = 0, \Gamma = 1$
(d) $\Delta = 0, \Gamma = 0$
(e) None of the above.

Problem 3.5. (5 points) Assume the Black-Scholes framework as model for the price of a non-dividend-paying stock. What is the difference between the delta of a European call option and the delta of the otherwise identical put option?
(a) 0
(b) 1
(c) $S(0)$
(d) Not enough information is given to answer this question.
(e) None of the above.

Problem 3.6. (2 points) Rho measures the sensitivity of a portfolio to the changes in the applicable risk-free interest rate. True or false?

Problem 3.7. (2 points) Market makers can partially insure themselves against possible losses by trading in the out-of-the-money options.

Problem 3.8. Let $S(0) = 100, K = 120, \sigma = 0.3, r = 0.08$ and $\delta = 0$.
(a) (8 pts) Let $V_C(0, T)$ denote the Black-Scholes European call price for the maturity $T$. Does the limit of $V_C(0, T)$ as $T \to \infty$ exist? If it does, what is it?
(b) (8 pts) Now, set $\delta = 0.001$ and let $V_C(0, T, \delta)$ denote the Black-Scholes European call price for the maturity $T$. Again, how does $V_C(0, T, \delta)$ behave as $T \to \infty$?
(c) (4 pts) Interpret in a sentence or two the differences, if there are any, between your answers to questions in a. and b.

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