

Problem 3. Give an exact answer for the following expressions:

a) $\tan(\sin^{-1}(-1/2))$

$$\sin \theta = -\frac{1}{2}$$

$$\theta = -\frac{\pi}{6}$$

$$\tan\left(-\frac{\pi}{6}\right) = -\frac{\sqrt{3}}{3}$$

b) $\csc(\cos^{-1}(1/3))$

$$\cos \theta = \frac{1}{3} \quad 0 < \theta < \frac{\pi}{2}$$

$$x = 1 \quad y = ?$$

$$x^2 + y^2 = r^2$$

$$1 + y^2 = 9$$

$$y = \sqrt{8} = 2\sqrt{2}$$

$$\csc \theta = \frac{r}{y} = \frac{3}{2\sqrt{2}} = \frac{3\sqrt{2}}{4}$$

c) $\tan^{-1}(\tan(7\pi/6))$

$$\tan^{-1}\left(\tan\left(\frac{7\pi}{6}\right)\right) = \tan^{-1}\left(\frac{\sqrt{3}}{3}\right) = \frac{\pi}{6}$$