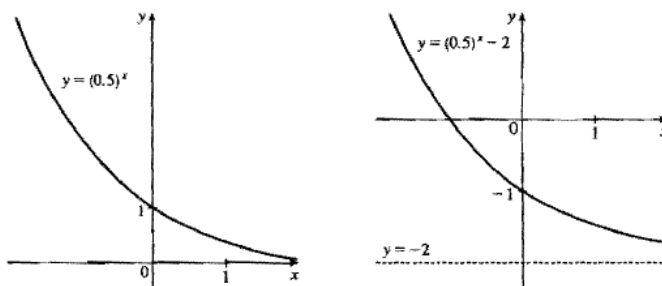


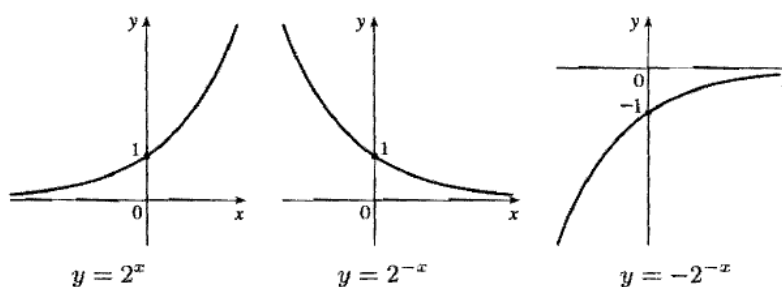
Homework 1

Section 1.5:

12. We start with the graph of $y = (0.5)^x$ (Figure 3) and shift it 2 units downward to obtain the graph of $y = (0.5)^x - 2$. The horizontal asymptote of the final graph is $y = -2$.



13. We start with the graph of $y = 2^x$ (Figure 2), reflect it about the y -axis, and then about the x -axis (or just rotate 180° to handle both reflections) to obtain the graph of $y = -2^{-x}$. In each graph, $y = 0$ is the horizontal asymptote.



19. (a) The denominator is zero when $1 - e^{1-x^2} = 0 \Leftrightarrow e^{1-x^2} = 1 \Leftrightarrow 1 - x^2 = 0 \Leftrightarrow x = \pm 1$. Thus, the function $f(x) = \frac{1 - e^{x^2}}{1 - e^{1-x^2}}$ has domain $\{x \mid x \neq \pm 1\} = (-\infty, -1) \cup (-1, 1) \cup (1, \infty)$.
- (b) The denominator is never equal to zero, so the function $f(x) = \frac{1 + x}{e^{\cos x}}$ has domain \mathbb{R} , or $(-\infty, \infty)$.

21. Use $y = Ca^x$ with the points $(1, 6)$ and $(3, 24)$. $6 = Ca^1$ [$C = \frac{6}{a}$] and $24 = Ca^3 \Rightarrow 24 = \left(\frac{6}{a}\right)a^3 \Rightarrow 4 = a^2 \Rightarrow a = 2$ [since $a > 0$] and $C = \frac{6}{2} = 3$. The function is $f(x) = 3 \cdot 2^x$.

24. Suppose the month is February. Your payment on the 28th day would be $2^{28-1} = 2^{27} = 134,217,728$ cents, or \$1,342,177.28. Clearly, the second method of payment results in a larger amount for any month.

Section 1.6:

6. No horizontal line intersects the graph more than once. Thus, by the Horizontal Line Test, the function is one-to-one.
8. We could draw a horizontal line that intersects the graph in more than one point. Thus, by the Horizontal Line Test, the function is not one-to-one.
16. First, we must determine x such that $f(x) = 3$. By inspection, we see that if $x = 1$, then $f(1) = 3$. Since f is 1-1 (f is an increasing function), it has an inverse, and $f^{-1}(3) = 1$. If f is a 1-1 function, then $f(f^{-1}(a)) = a$, so $f(f^{-1}(2)) = 2$.

18. (a) f is 1-1 because it passes the Horizontal Line Test.

(b) Domain of $f = [-3, 3] = \text{Range of } f^{-1}$. Range of $f = [-1, 3] = \text{Domain of } f^{-1}$.

(c) Since $f(0) = 2$, $f^{-1}(2) = 0$.

(d) Since $f(-1.7) \approx 0$, $f^{-1}(0) \approx -1.7$.

30. Reflect the graph of f about the line $y = x$.

