Introduction to Applied Harmonic Analysis
Fall 2016

Course: M 393C / CSE 396
Time/location: Tuesday & Thursday 9:30 - 11:00 AM (RLM 11.176)

Instructor: Rachel Ward
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Office Hours: T/Th 11AM-noon, or by appointment

Target Audience: Graduate students in Math, ECE, ICES, CS, DSSC, and advanced undergraduate students

Class webpage: www.ma.utexas.edu/~rward/courses/ACHA16.htm

Course Objective: This course should serve as an introduction to mathematical building blocks from time-frequency analysis (e.g. Fourier series, wavelets, sampling theorems) that can be used for signal and image processing, numerical analysis, and statistics. The course will emphasize the connection between the analog world and the discrete world, and focus on approximation and compression of functions and data. We will also discuss recent advances in sparse representations and compressive sensing.

Prerequisites: Linear algebra (M341 or equivalent), probability (M362K or equivalent), real analysis (M365C or equivalent), functional analysis or second-semester real analysis, or consent of instructor.

Topics:
- Fourier Transforms, Sampling Theorems, Fourier Series
- Discrete Fourier Transform, Discrete Cosine Transform
• The Uncertainty Principle and Bandlimited Signals
• Frame Theory
• Tools using Time/Frequency Domain Partitioning
  o Local Cosine/Sine Transform
  o Fast Laplace/Poisson Solvers
  o Haar Wavelets
  o Multiresolution Analysis
  o Discrete Wavelet Transform
  o Image Approximation / Compression
• Principal Component Analysis
• Sparsity / Compressive Sensing

Textbooks:
- Required:

- Optional:

Grading Scheme: 50% Homework / participation.
50% Final project

Homework: Homework will be assigned every three weeks, and include proof-based and Matlab-based exercises. Additional problems will be presented during lectures, and students will present solutions to these problems during class.
Tentative Schedule:

- Thursday, Aug. 25: Introduction/ Overview
- Tuesday, Aug. 30: Basics of Fourier Transforms I
- Thursday, Sept. 1: Basics of Fourier Transforms II
- Tuesday, Sept. 6: Uncertainty Principles
- Thursday, Sept. 8: Discussion
- Tuesday, Sept. 13: Discretization via Sampling
- Thursday, Sept. 15: Fourier Series on Intervals
- Tuesday, Sept. 20: Functions of Bounded Variation
- Thursday, Sept. 22: Discrete Fourier Transform
- Tuesday, Sept. 27: Fast Fourier Transform
- Thursday, Sept. 29: Poisson Summation Formula
- Tuesday, Oct. 4: Compressive sensing
- Thursday, Oct. 6: Compressive sensing
- Tuesday, Oct. 11: Compressive sensing
- Thursday, Oct. 13: Compressive sensing
- Tuesday, Oct. 18: Compressive sensing
- Thursday, Oct. 20: Frame Theory
- Tuesday, Oct. 25: Wavelets/ Short time Fourier Transform
- Thursday, Oct. 27: Wavelets
- Tuesday, November 1: Fast Wavelet Transform
- Nov 3. – Nov. 22: FINAL PRESENTATIONS
- Nov. 29 – Dec. 1: Whatever is left

**Lectures will often follow the notes of Naoki Saito at https://www.math.ucdavis.edu/~saito/courses/ACHA.w14/lectures.html**