

$$\cos \theta = \sqrt{1-x^2}$$

$$\cos(\phi) = x$$

$$\phi = \frac{\pi}{2} - \theta$$

$$\phi = \cos^{-1}(x) = \frac{\pi}{2} - \sin^{-1}(x)$$

$$\theta = \sin^{-1}(x)$$

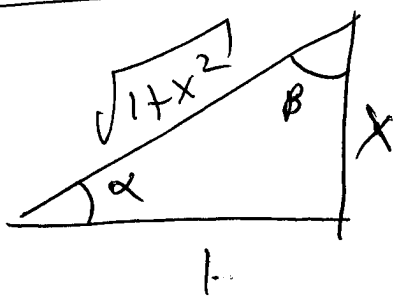
$$\cos(\sin^{-1}(x)) = \sqrt{1-x^2}$$

$$\tan(\sin^{-1}(x)) = \frac{x}{\sqrt{1-x^2}}$$

$$\cot = \frac{\sqrt{1-x^2}}{x}$$

$$\sec = \frac{1}{\sqrt{1-x^2}}$$

$$\csc = \frac{1}{x}$$



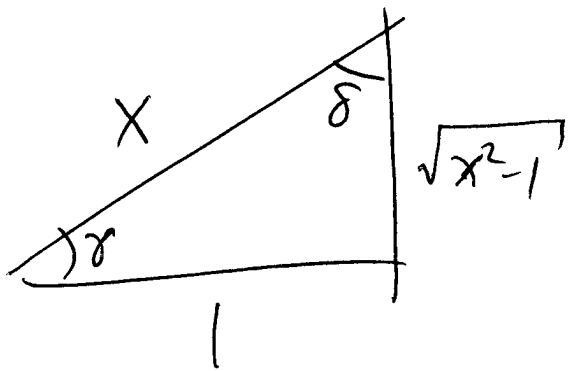
$$\tan(\alpha) = x$$

$$\alpha = \tan^{-1}(x)$$

$$\cot(\beta) = x$$

$$\beta = \cot^{-1}(x) = \frac{\pi}{2} - \alpha$$

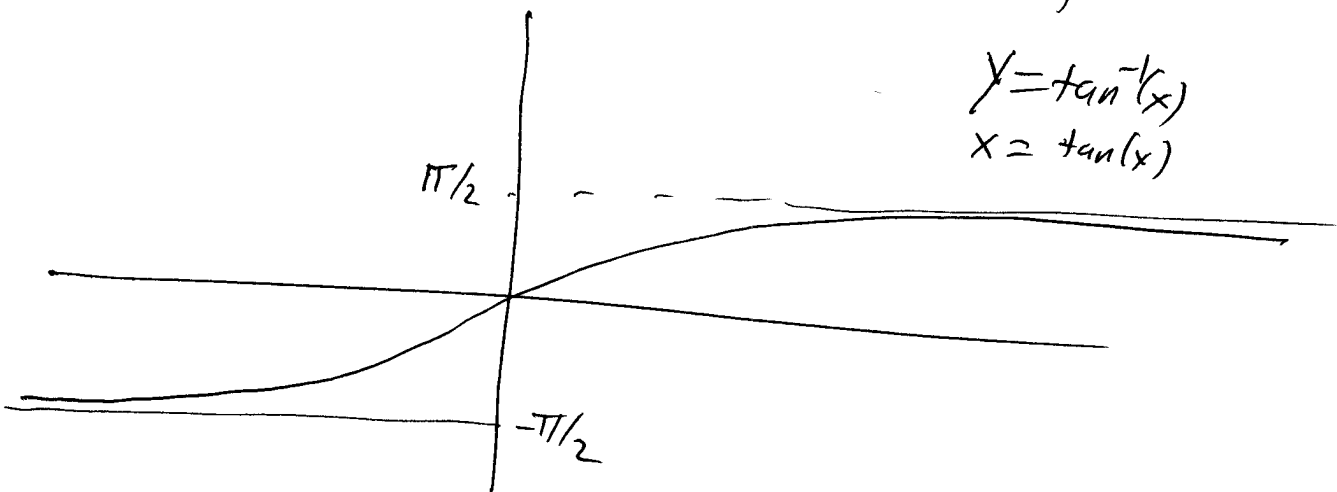
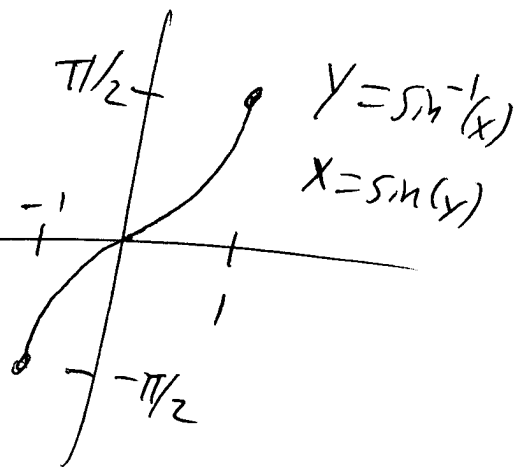
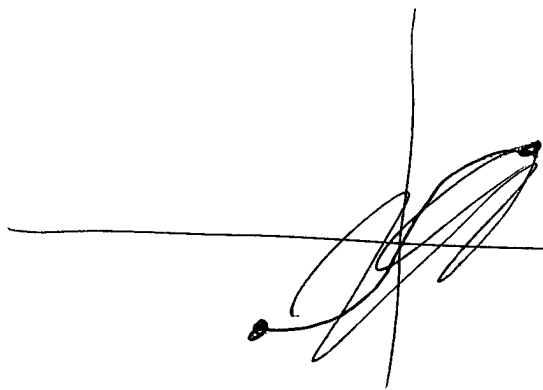
$$= \frac{\pi}{2} - \tan^{-1}(x)$$

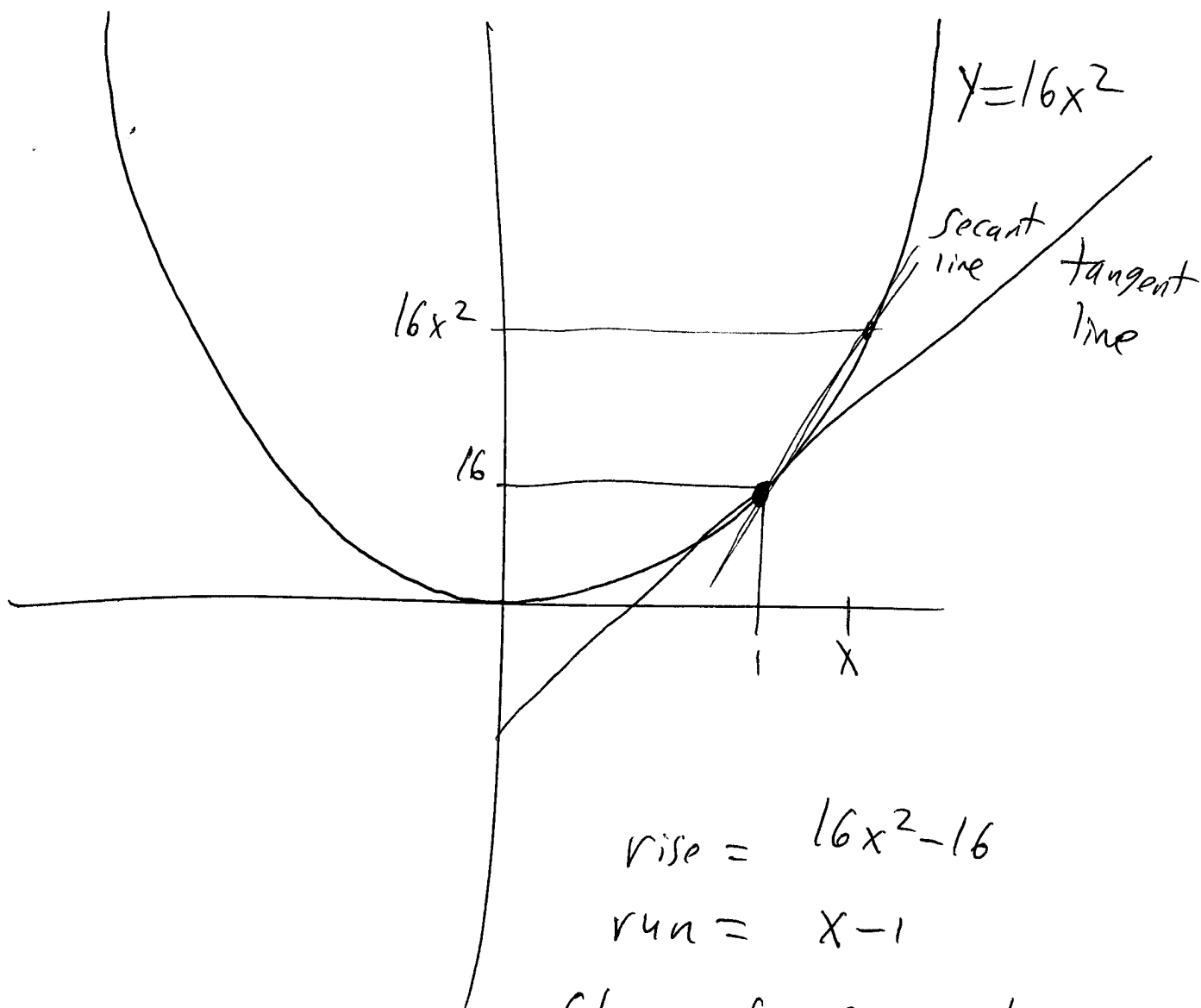


$$\sec \theta = x$$

$$\theta = \sec^{-1}(x)$$

$$\theta = \csc^{-1}(x) = \frac{\pi}{2} - \sec^{-1}(x)$$





$$\text{rise} = 16x^2 - 16$$

$$\text{run} = x - 1$$

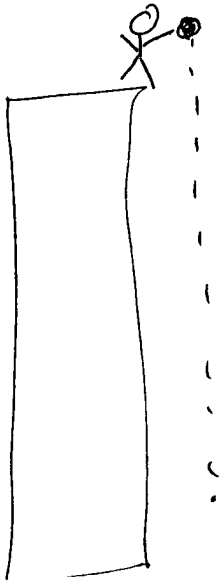
Slope of Secant line

$$= \frac{16x^2 - 16}{x - 1}$$

x	$\frac{16x^2 - 16}{x - 1}$
2	48
1.5	40
1.1	33.6
1.01	32.16
1.001	32.016

Slope of tangent line.

$$= \lim_{x \rightarrow 1} \frac{16x^2 - 16}{x - 1}$$



$X = \text{distance it fall}$

$$X = 16t^2$$

t	X
0	
.98	
.99	
1	16
1.01	16.3216
1.1	19.36
1.5	36
2	64

instantaneous
velocity at
 $t=1$

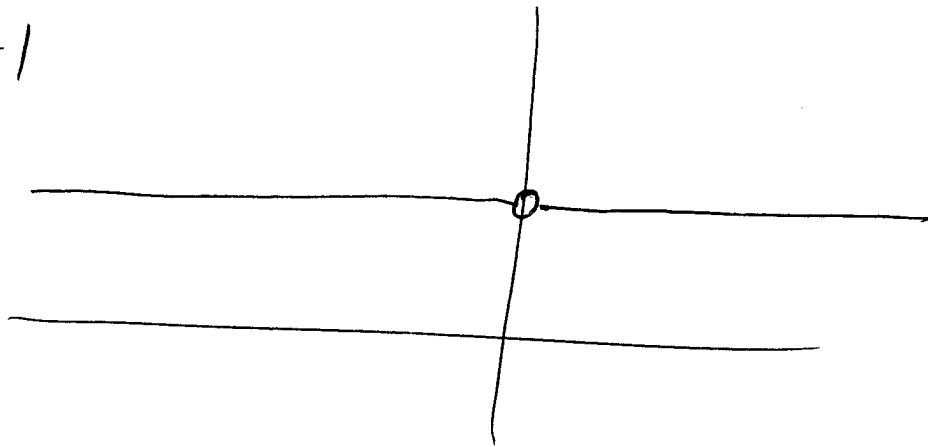
$$= \lim_{t \rightarrow 1} \frac{16t^2 - 16}{t - 1}$$

16
1.21
~~16~~
32

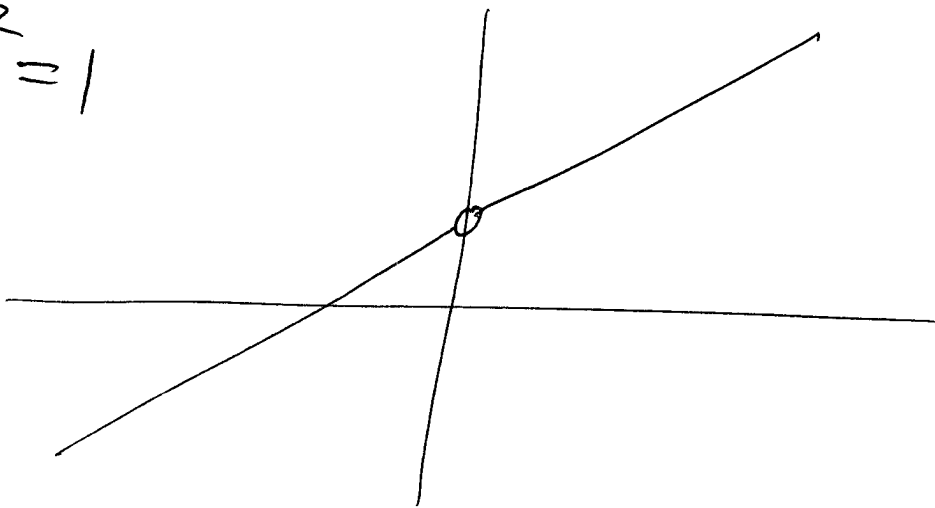
" $\lim_{x \rightarrow a} f(x) = L$ " means

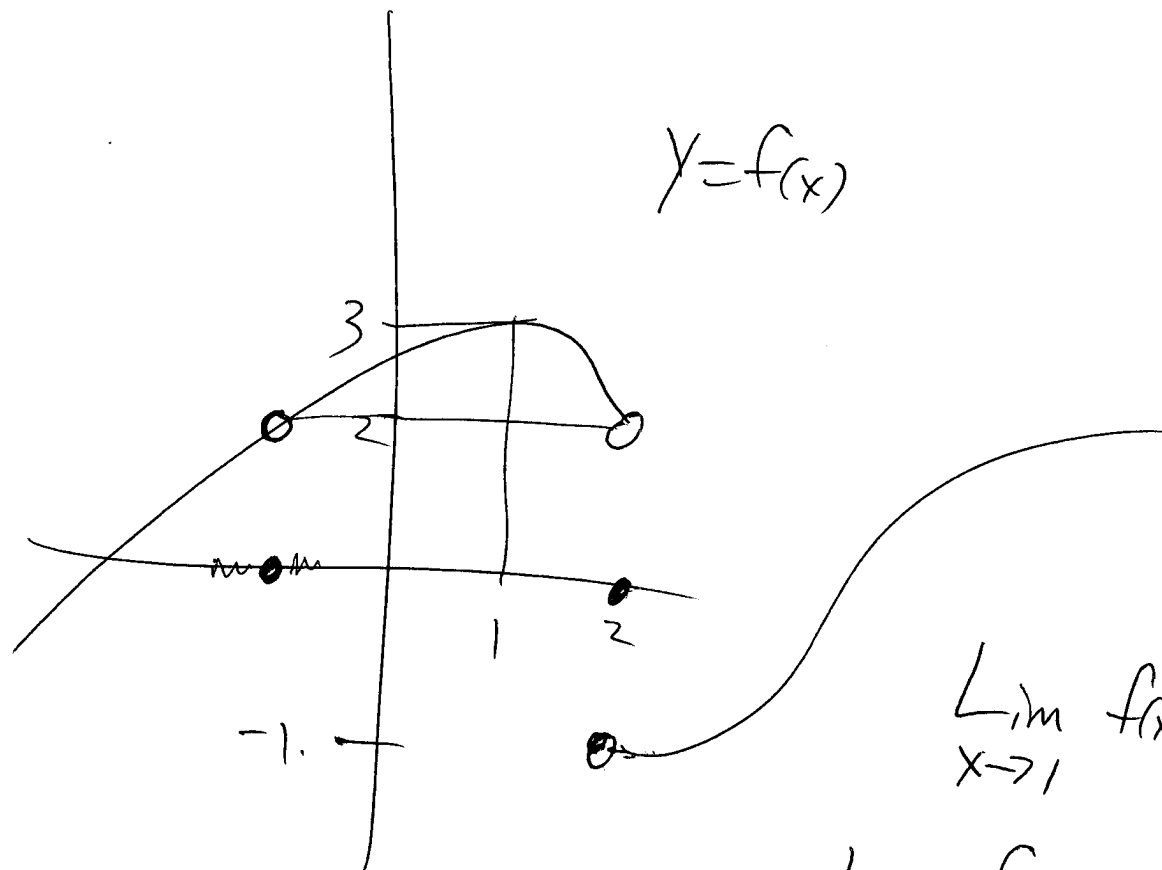
"Whenever x is close to a (but not $=a$)
 $f(x)$ is close to L "

$$\lim_{x \rightarrow 0} \frac{x}{x} = 1$$



$$\lim_{x \rightarrow 0} \frac{x+x^2}{x} = 1$$





$$y=f(x)$$

$$\lim_{x \rightarrow 1} f(x) = 3$$

$$\lim_{x \rightarrow 2} f(x) = \text{DNE}$$

$$\lim_{x \rightarrow -1} f(x) = 2$$

$$\lim_{x \rightarrow 2^-} f(x) = 2$$

$$\lim_{x \rightarrow 2^+} f(x) = -1$$

One-sided limits.

$$\text{"} \lim_{x \rightarrow a^-} f(x) = L \text{"}$$

means

"Whenever x is slightly less than a , then $f(x)$ is close to L "

$$\text{"} \lim_{x \rightarrow a^+} f(x) = L \text{"}$$

means

"Whenever x is slightly bigger than a , $f(x)$ is close to L "

" $\lim_{x \rightarrow a} f(x) = +\infty$ " means

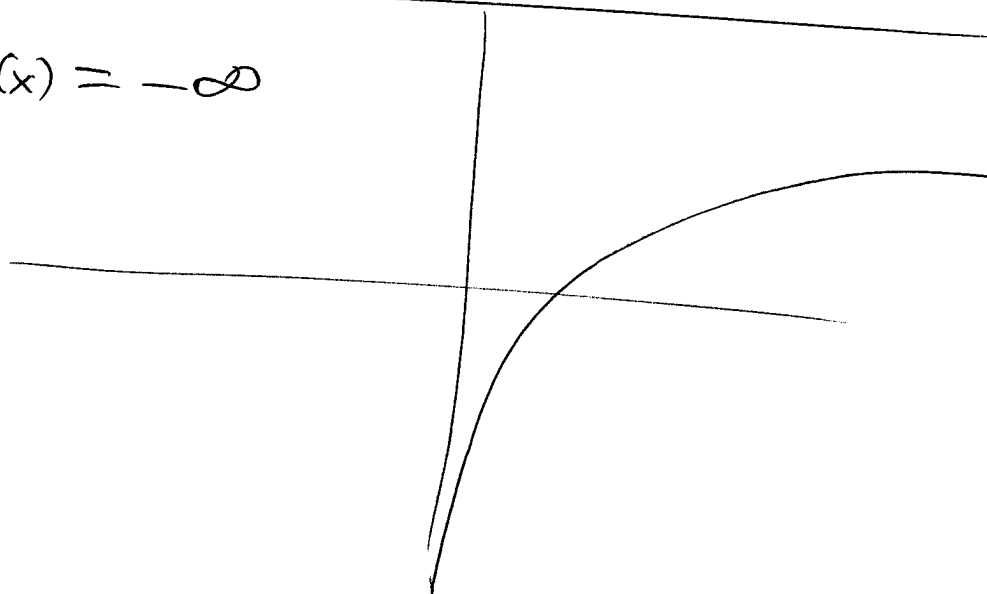
" Whenever x is close to a , $f(x)$ is large & positive
(but not $= a$)

$$\lim_{x \rightarrow 0} \frac{1}{x^2} = +\infty$$

$$\lim_{x \rightarrow 0^+} \frac{1}{x} = +\infty$$

$$\lim_{x \rightarrow 0^-} \frac{1}{x} = -\infty$$

$$\lim_{x \rightarrow 0^+} \ln(x) = -\infty$$



" $\lim_{x \rightarrow \infty} f(x) = L$ " means

"Whenever x is large & positive, $f(x) \approx L$ "

$$\lim_{x \rightarrow \infty} \tan^{-1}(x) = \pi/2$$

" $\lim_{x \rightarrow -\infty} f(x) = L$ " means

"Whenever x is large & neg, $f(x) \approx L$ "

$$\begin{array}{l} \lim_{x \rightarrow a} f(x) = L \\ x \rightarrow a \\ x \rightarrow a^+ \\ x \rightarrow a^- \\ x \rightarrow \infty \\ x \rightarrow -\infty \end{array}$$