

Let  $F$  be the free group on two generators  $x$  and  $y$ . Let  $N$  be the smallest normal subgroup of  $F$  containing  $y$  and  $H = \langle x \rangle$ . Show that  $F$  is the semidirect product of  $N$  and  $H$ .