

FINDING THE TAYLOR SERIES OF $f(x) = \sin x$
Centered at $a = \pi/2$

Here $a = \pi/2$, $c_n = \frac{f^{(n)}(\pi/2)}{n!}$ and $c_n (x-a)^n = \frac{f^{(n)}(\pi/2)}{n!} (x - \pi/2)^n$

Use k:	n	$f^{(n)}(x)$	$f^{(n)}(\pi/2)$	$c_n (x-a)^n$
$k=0$	0	$\sin x$	$\sin(\pi/2) = 1$	$\frac{1}{0!} (x - \pi/2)^0 = 1$
	1	$\cos x$	$\cos(\pi/2) = 0$	
$k=1$	2	$-\sin x$	$-\sin(\pi/2) = -1$	$\frac{-1}{2!} (x - \pi/2)^2$
	3	$-\cos x$	$-\cos(\pi/2) = 0$	
$k=2$	4	$\sin x$	$\sin(\pi/2) = 1$	$\frac{1}{4!} (x - \pi/2)^4$
	5	$\cos x$	$\cos(\pi/2) = 0$	
$k=3$	6	$-\sin x$	$-\sin(\pi/2) = -1$	$\frac{-1}{6!} (x - \pi/2)^6$
	\vdots	\vdots	\vdots	\vdots

$$\sin x = \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k)!} (x - \pi/2)^{2k}$$

It can be shown that the radius of convergence is $R = \infty$.